## Quadratic inequalities

## A LEVEL LINKS

Scheme of work: 1d. Inequalities - linear and quadratic (including graphical solutions)

## Key points

- First replace the inequality sign by $=$ and solve the quadratic equation.
- Sketch the graph of the quadratic function.
- Use the graph to find the values which satisfy the quadratic inequality.


## Examples

Example 1 Find the set of values of $x$ which satisfy $x^{2}+5 x+6>0$

| $\begin{aligned} & x^{2}+5 x+6=0 \\ & (x+3)(x+2)=0 \\ & x=-3 \text { or } x=-2 \end{aligned}$ <br> It is above the $x$-axis <br> This part of the graph is not needed as this is where $x^{2}+5 x+6<0$ $x<-3 \text { or } x>-2$ | 1 Solve the quadratic equation by factorising. <br> 2 Sketch the graph of $y=(x+3)(x+2)$ <br> 3 Identify on the graph where $x^{2}+5 x+6>0$, i.e. where $y>0$ |
| :---: | :---: |
|  | 4 Write down the values which satisfy the inequality $x^{2}+5 x+6>0$ |

Example 2 Find the set of values of $x$ which satisfy $x^{2}-5 x \leq 0$

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| $x^{2}-5 x=0$ <br> $x(x-5)=0$ <br> $x=0$ or $x=5$ <br> $y \uparrow$ | 1 <br> Solve the quadratic equation by <br> factorising. |
| :--- | :--- | :--- |

Example 3 Find the set of values of $x$ which satisfy $-x^{2}-3 x+10 \geq 0$


## Practice

1 Find the set of values of $x$ for which $(x+7)(x-4) \leq 0$

2 Find the set of values of $x$ for which $x^{2}-4 x-12 \geq 0$

3 Find the set of values of $x$ for which $2 x^{2}-7 x+3<0$

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4 Find the set of values of $x$ for which $4 x^{2}+4 x-3>0$

5 Find the set of values of $x$ for which $12+x-x^{2} \geq 0$

## Extend

Find the set of values which satisfy the following inequalities.
$6 \quad x^{2}+x \leq 6$
$7 x(2 x-9)<-10$
$8 \quad 6 x^{2} \geq 15+x$

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## Answers

1

2

3
$x \leq-2$ or $x \geq 6$
$\frac{1}{2}<x<3$

4

5

6
$72<x<2^{\frac{1}{2}}$
$8 \quad x \leq-\frac{3}{2}$ or $x \geq \frac{5}{3}$

